# Conformational Analysis. Part 12.¹ A Theoretical and Lanthanide-induced Shift (LIS) Investigation of the Conformation of Benzophenone and 3,4'-Dichlorobenzophenone 

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#### Abstract

Conformational analysis of benzophenone and 3,4'-dichlorobenzophenone has been studied by theoretical (semiempirical and $a b$ initio) calculations and by the lanthanide-induced shift (LIS) technique. The theoretical calculations were based on ab initio (STO-3G) energies of MNDO optimised geometries. The minimum-energy conformer is a helical conformer with a dihedral angle ( $\theta$ ) between the phenyl and carbonyl group planes of $36^{\circ}$. Analysis of the theoretical curves gave a two-fold potential barrier about this bond of $20.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and further showed that the most likely rotation of the phenyl rings was via a disrotatory mechanism with a high-energy perpendicular intermediate $\left(\theta_{1}=0^{\circ}, \theta_{2}=90^{\circ}\right) 5.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$ above the ground state. The LIS investigation of benzophenone was inconclusive due to the molecular symmetry, all torsional angles giving good solutions. For the 3,4'-dichlorobenzophenone the more extensive data set allowed a precise analysis. The best agreement factor was found for $56 \%$ of the trans conformer with a torsional angle ( $\theta$ ) of $26^{\circ}$. The lanthanide was also unevenly populated about the carbonyl group, $55 \%$ being on the side of the meta-chloro ring, with values of $r, \varphi$, and $\psi$ for the Ln-O geometry found to be $2.75 \AA$, 55$60^{\circ}$ and $160-165^{\circ}$, respectively. These results can be explained on the basis of steric effects between the lanthanide and the phenyl rings rogether with different $\pi$ densities in the two rings.


The conformation of benzophenone has been studied by a wide variety of experimental and theoretical methods, all of which have indicated the preferred conformation to be helical (rings twisted out of the central carbonyl plane in opposite directions) rather than gable (rings twisted in similar directions) ${ }^{2}$ (Figure 1). A third conformational form has also been suggested, ${ }^{3}$ having one ring planar to the carbonyl and the other ring twisted out of the plane by a large angle (about $70^{\circ}$ ). However, the experimental evidence is overwhelmingly in favour of the helical form with each ring twisted from the plane by the same angle, $\theta_{1}$ and $\theta_{2}$, respectively. The degree of twist is less certain, values ranging from $42^{\circ}$ (from molar Kerr constants) ${ }^{3}$ to $30^{\circ}$ (by $X$-ray diffraction). ${ }^{4}$ Similarly various theoretical treatments have failed to produce a constant value. An extended Hückel (EH) approach ${ }^{5}$ gave a minimum-energy helical conformation having a twist angle of $38^{\circ}$, a CNDO/ 2 study by the same workers indicated the favoured conformation to be $\theta_{1}=\theta_{2}=$ $90^{\circ}$. The tendency of NDO methods to fail for conjugated systems was more recently demonstrated by a study using MINDO/3, MNDO, and MNDOC, all of which indicated the low-energy conformer to be helical with twist angles of 89.7 , 70.4 , and $77.9^{\circ}$, respectively. ${ }^{6}$ Very small energy differences were found between these conformers and the $\theta_{1}=\theta_{2}=90^{\circ}$ conformer, only $1.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$ in the MNDO case and close to zero in the remainder. This is in contrast with an energy barrier of $14.1 \mathrm{~kJ} \mathrm{~mol}^{-1}$ for rotation via the $90^{\circ}$ conformer found by the
(a)

(b)


Figure 1. (a) Helical and (b) gable forms of benzophenone

EH study. A recent evaluation of the energy barrier to rotation ${ }^{7}$ using ${ }^{13} \mathrm{C}$ spin lattice relaxation times ( $T_{1}$ ) produced a value of $11.5 \mathrm{~kJ} \mathrm{~mol}^{-1}$. Rotation may not be occurring via the $90^{\circ}$ conformer, however, indeed a modified C-INDO study ${ }^{2}$ (which, in contrast to the above NDO methods, gave good agreement with experimental determinations of the twist angle--a value of $30^{\circ}$ being indicated) suggested rotation would occur via the $\theta_{1}=0^{\circ}, \theta_{2}=90^{\circ}$ conformer.

Substituents in the 3 and 4 positions have generally been found to exert little influence on the preferred conformation, either in solution, ${ }^{8.9}$ or in the solid phase, an $X$-ray study of $4,4^{\prime}$-dichlorobenzophenone ${ }^{10}$ produced a twist angle of $29^{\circ}$ (compared with $30^{\circ}$ reported earlier for benzophenone). Generally, twist angles determined by similar methods have been of the same order for the parent molecule and substituted benzophenones. Grimaud et al. ${ }^{9}$ carried out an extensive experimental study using a variety of techniques including optical anisotropy determinations, infra-red studies, and some lanthanide shift work [using $\mathrm{Eu}(\mathrm{dpm})_{3}$ and proton spectra only]. The first of these methods ${ }^{9 a, 9 b}$ produced a twist angle of $31 \pm 1^{\circ}$ for benzophenone itself and a series of similar values for a number of chloro-substituted derivatives; $27^{\circ}$ for the $4,4^{\prime}$ dichloro, $31.5^{\circ}$ for the 4 -chloro, and $31.5^{\circ}$ for the 3 -chloro. An interesting observation from the lanthanide study of $3,3^{\prime}-$ dichlorobenzophenone ${ }^{9 c}$ was an apparent conformational preference for the trans conformer (with respect to the chlorine positions relative to the carbonyl) over the cis isomer (52$48 \%$ ). The indicated twist angle in this case was $37^{\circ}$.

Our interest in the molecule results from the presence of a benzophenone-like unit in the commercially important poly(aryl ether ketone) polymers. In order to achieve reliable molecular modelling of the polymer chain it is necessary to know both the geometry and torsional potential around the phenylcarbonyl bonds. We present here both theoretical and experimental approaches to this problem, the theoretical via semiempirical (MNDO) and $a b$ initio (STO-3G) calculations and the experimental via the lanthanide-induced shift technique.

Table 1. MNDO optimised geometry parameters and MNDO and STO-3G energies for helical ${ }^{a}$ conformations of benzophenone
$\theta_{1}\left(=\theta_{2}\right)^{a}$

angle $\left({ }^{\circ}\right)$$c$| $\mathrm{C}=\mathrm{O}$ bond |
| :---: |
| length $(\AA)$ |

| $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ bond <br> length $(\AA)$ | $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ <br> angle $\left(^{\circ}\right)$ |
| :---: | :---: |
| 1.542 | 135.71 |
| 1.536 | 133.25 |
| 1.524 | 127.75 |
| 1.518 | 123.14 |
| 1.514 | 120.15 |
| 1.511 | 118.76 |
| 1.510 | 118.04 |
| 1.510 | 117.61 |
| 1.510 | 117.46 |
| 1.510 | 117.41 |
| 1.532 | 132.48 |
| 1.518 | 123.08 |


| MNDO $^{b}$ <br> energy | STO-3G <br> energy |
| :---: | :---: |
| 104.8 | 67.8 |
| 89.8 | 53.3 |
| 58.2 | 23.5 |
| 32.2 | 6.2 |
| 17.6 | 5.0 |
| 10.1 | 10.7 |
| 6.6 | 17.7 |
| 5.3 | 23.8 |
| 5.0 | 28.2 |
| 5.0 | 29.9 |
| 76.0 | 54.7 |
| 24.9 | 32.5 |

${ }^{a}$ Unless indicated otherwise. ${ }^{b}$ Quoted energy $=(M \times 96.485)+5.0 \mathrm{~kJ} \mathrm{~mol}^{-1}$, where $M$ is the energy difference (in eV) between a conformer and the $80.0^{\circ}$ form. ${ }^{c}$ Quoted energy $=(G \times 2625.01)+5.0 \mathrm{~kJ} \mathrm{~mol}^{-1}$, where $G$ is the energy difference (in a.u.) between a conformer and the $40.0^{\circ}$ form. ${ }^{d}$ Gable conformation: (1) $\theta_{1}=30^{\circ}, \theta_{2}=150^{\circ}$, (2) $\theta_{1}=60^{\circ}, \theta_{2}=120^{\circ}$.


Figure 2. Illustration of method of ring rotation used in the theoretical study


Figure 3. Energy $v s$. conformation for benzophenone
Conformational analysis of molecules in solution by means of lanthanide-induced shifts is a well established technique which has been applied to a wide variety of substrates. ${ }^{11,12}$ The method involves the experimental determination of pseudocontact shift values ( $\delta \Delta$ ) for both $\mathbf{C}$ and $\mathbf{H}$ atoms, these values generally being quoted for a lanthanide shift reagent ( L ): substrate (S) molar ratio of $1: 1(\rho=[\mathrm{L}] /[\mathrm{S}]=1)$. Experimentally values of $\rho \leqslant 0.2$ are used, since in this region the $\rho v s$. observed shift relationship is a linear one and $\delta \Delta$ can be
obtained from the slope of this plot. The LIS $(\Delta M)$ is not purely a pseudo-contact shift but contains contributions from two other sources, namely a contact shift [considered negligible for $\mathrm{Yb}(\mathrm{fod})_{3}$ ] and a diamagnetic shift $(\Delta D)$ [estimated from shifts obtained with complexation of $\mathrm{La}(\mathrm{fod})_{3}$ for C atoms, but considered negligible for H atoms].

The $\Delta M-\Delta D$ values obtained from the above method are then compared with those calculated from the McConnellRobertson equation ${ }^{13}$ where $r_{i}$ is the distance between the

$$
\begin{equation*}
\delta \Delta=x\left(3 \cos ^{2} \theta-1\right) / r_{\mathrm{i}}{ }^{3} \tag{1}
\end{equation*}
$$

lanthanide and atom $\mathrm{i}, x$ is a constant for the system, and $\theta$ is the O - Ln -atom i angle for various conformations of the substratelanthanide complex. The method can provide information on the molecular conformation and conformational isomerism in solution.

## Theoretical

(i) Preferred Conformation of Benzophenone.-Analyses using the MNDO method ${ }^{14,15}$ and GAUSSIAN76 (STO-3G basis set ${ }^{16.17}$ were carried out, the results of which are presented in Table 1. Ring rotations are measured as angles of twist from the planar form where $\theta_{1}$ is the degree of twist of ring 1 in a clockwise direction [as viewed from $C(1)$ to $C(O)$ ] and $\theta_{2}$ is the degree of twist of ring 2 in an anticlockwise direction [viewed from $C(O)$ to $C\left(1^{\prime}\right)$ ], see Figure 2.
An initial MNDO optimisation of the $\mathrm{C}=\mathrm{O}$ and $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ bond lengths and the $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ bond angle produced a geometry which was then used in the GAUSSIAN76 programme. Little change is seen in these parameters for all conformations other than in those approaching planarity (see Table 1). As expected, MNDO predicts a preferred conformer with twist angle close to $90^{\circ}$. The result, similar to that observed in a previous study, ${ }^{6}$ is an example of the failure of MNDO to correctly account for conjugation energy. STO-3G, in contrast, predicted a well defined minimum-energy conformation with a twist angle of $36^{\circ}$ (see Figure 3), corresponding to an energy of $4.3 \mathrm{~kJ} \mathrm{~mol}^{-1}$ on the STO-3G scale used in Table 1. The MNDO optimised parameters for this conformer were $1.230 \AA(\mathrm{C}=\mathrm{O})$, $1.515 \AA[\mathrm{C}(\mathrm{O})-\mathrm{C}(1)]$, and $121.28^{\circ} \mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$.
Similar calculations were performed for the $30^{\circ}$ and $60^{\circ}$ gable conformers $\left(\theta_{1}=30^{\circ}, \theta_{2}=150^{\circ}\right.$ and $\theta_{1}=60^{\circ}, \theta_{2}=120^{\circ}$, respectively). Both MNDO and STO-3G predict these forms to be considerably higher in energy than the equivalent helical forms, the expected result (Table 1).


Figure 4. Energy barrier to ring rotation by a conrotatory mechanism using MNDO $\left(\theta_{1}=80^{\circ}\right)$ and GAUSSIAN76 $\left(\theta_{1}=36^{\circ}\right)$


Figure 5. Energy barrier to ring rotation by a disrotatory mechanism using MNDO $\left[\left(90-\theta_{1}\right)+\left(90-\theta_{2}\right)=20^{\circ}\right]$ and GAUSSIAN76 $\left[\left(90-\theta_{1}\right)+\left(90-\theta_{2}\right)=108^{\circ}\right]$

The above calculations were carried out assuming no change would occur in the geometry of the rings on rotation. In practice this is found to be incorrect, as the following calculation on the planar conformer indicates. MNDO optimisation of the $\mathrm{C}(\mathrm{O})-\mathrm{C}(1)-\mathrm{C}(2)$ and $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{H}(1)$ angles (in addition to those parameters previously optimised) produced values of $124.72^{\circ}$ and $123.33^{\circ}$, respectively. A value of $130.42^{\circ}$ was indicated for the $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ angle, considerably smaller than that given by the more rigid optimisation ( $135.71^{\circ}$ ). The STO-3G energy of this geometry was calculated to be 44.6 kJ $\mathrm{mol}^{-1}$, some $23.2 \mathrm{~kJ} \mathrm{~mol}^{-1}$ lower than that found for the more rigid planar conformer. However, this conformation is by far the highest in energy and thus similar calculations performed on other conformers might be expected to produce less significant differences, indeed for conformations where steric effects are
small no significant energy difference between the two methods is likely to be observed. Since it is these latter conformations which are of importance in the following consideration of energy barriers (the planar conformer is a very unlikely intermediate) and rotational potentials the more rigid optimisations are considered to give an adequate assessment of the total energy.
(ii) Energy Barrier to Ring Rotation.-There are two possible mechanisms by which ring rotation in benzophenone may occur, involving either conrotatory or disrotatory movement of the rings. Figure 3 is an example of one conrotatory model; both MNDO and STO-3G indicate that the rotation will occur via the $\theta_{1}=\theta_{2}=90^{\circ}$ conformer, rather than through the planar conformer. However, whilst STO-3G suggests a barrier of some $25 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ( $6 \mathrm{kcal} \mathrm{mol}^{-1}$ ), MNDO predicts the same barrier to be close to zero.

The conrotatory mechanism was further studied by using the preferred conformers from the previous section. With $\theta_{1}$ fixed at $80^{\circ}$ and $36^{\circ}$ for the MNDO and STO-3G studies, respectively, a similar MNDO optimisation to that used in the previous section [optimisation of $\mathrm{C}=\mathrm{O}$ and $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ bond lengths and the $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ angle] was carried out for a series of $\theta_{2}$ angles from $0-180^{\circ}$. STO-3G energies were then calculated for the optimised geometries of the $\theta_{1}=36^{\circ}$ conformers. The results of this analysis are presented in Figure 4.

Barriers to rotation, as shown in Figure 4, are predicted to be $15.5 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ( $3.7 \mathrm{kcal} \mathrm{mol}^{-1}$ ) by MNDO and $47 \mathrm{~kJ} \mathrm{~mol}^{-1}(11.2$ $\mathrm{kcal} \mathrm{mol}{ }^{-1}$ ) by STO-3G. The poor agreement in the height of the energy barrier is further compounded by the difference in the conformations predicted to be the high-energy forms. MNDO suggests the $\theta_{1}=80^{\circ}, \theta_{2}=170^{\circ}$ (equivalent to a gable conformation of twist angles 80 and $10^{\circ}$ ) is of highest energy whereas STO-3G indicates the $\theta_{1}=36^{\circ}, \theta_{2}=150^{\circ}$ (gable conformation, angles of 36 and $30^{\circ}$ ) conformer is the higherenergy form. The gable conformer with $\theta_{2}=180-\theta_{1}$ might have been expected to be of highest energy; however, this is found to be less energetic than the above conformations by 13.1 $\mathrm{kJ} \mathrm{mol}^{-1}$ (MNDO) and by $1.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$ (STO-3G). The latter result seems more reasonable and it is interesting that the $\theta_{2}=$ $180-\theta_{1}$ form is close to, but not at, the high-energy point. A similar conclusion was reached for the conrotatory mechanism proceeding by the $\theta_{1}=\theta_{2}=90^{\circ}$ conformer. ${ }^{1}$

The disrotatory mechanism could involve the perpendicular conformation ( $\theta_{1}=0^{\circ}, \theta_{2}=90^{\circ}$ ) as the intermediate. MNDO predicts a barrier of $13.6 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and STO-3G one of 5.4 kJ $\mathrm{mol}^{-1}$ for this model.

A further possibility is for rotation to occur so as to maintain a similar angle between the rings to that found in the preferred conformer ( $20^{\circ}$ by MNDO, $108^{\circ}$ by STO-3G). The results of this analysis, carried out in a similar manner to those previously described, are shown in Table 2 and Figure 5. Once again only small variations were seen in the MNDO optimised bond lengths of conformers in the STO-3G study; however in the MNDO study some lengthening did occur from initial values of $1.224 \AA(\mathrm{C}=\mathrm{O})$ and $1.510 \AA[\mathrm{C}(1)-\mathrm{C}(\mathrm{O})]$ in the $80^{\circ}$ helical conformer to $1.237 \AA$ and $1.537 \AA$ in the conformer with each ring twisted $90^{\circ}$ from the initial position. Since this latter conformation is close to planarity this behaviour is entirely consistent with that seen in section (i).

Both MNDO and STO-3G predict that the high-energy conformer of the disrotatory model will be one in which the rings are twisted $90^{\circ}$ from their positions in the $80^{\circ}$ (MNDO) and $36^{\circ}$ (STO-3G) helical conformers. In the MNDO case this is very much the expected result since this is also the conformer which is closest to planarity, it is equivalent to a helical conformation of $\theta_{1}=\theta_{2}=10^{\circ}$. Given the already mentioned failing of MNDO to account for conjugation it is not surprising that the energy barrier predicted, $84.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$, is excessively

Table 2. Energy barriers to ring rotation by a disrotatory mechanism, MNDO and STO-3G studies. MNDO optimised $\mathrm{C}=\mathrm{O}^{a}$ and $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})^{b}$ bond lengths and $C(1)-C(O)-C\left(1^{\prime}\right)$ angle for each conformation

| MNDO |  |  |  |
| :---: | :---: | :---: | :---: |
| $\theta_{1}$ | $\theta_{2}$ | $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ | Energy ${ }^{\text {c }}$ |
| 80.0 | 80.0 | 117.46 | 5.0 |
| 95.0 | 65.0 | 118.44 | 9.0 |
| 110.0 | 50.0 | 121.68 | 22.2 |
| 125.0 | 35.0 | 126.40 | 43.0 |
| 140.0 | 20.0 | 130.28 | 65.6 |
| 155.0 | 5.0 | 132.48 | 83.1 |
| 170.0 | $-10.0$ | 133.22 | 89.8 |


$\overbrace{\theta_{1}} \quad$| 4 |
| :---: |
| $\theta_{2}$ |$\quad$| C(1)-C(O)-C(1') |
| :---: |${\text { Energy }{ }^{\text {d }}}^{\text {STO-3G }}$

${ }^{a} 1.230 \pm 0.007 \AA$ (MNDO), $1.228 \pm 0.003 \AA$ (STO-3G). ${ }^{b} 1.524 \pm 0.014 \AA$ (MNDO), $1.514 \pm 0.003 \AA$ (STO-3G). ${ }^{c}$ Based on similar scale to that used for MNDO energies in Table 1. ${ }^{d}$ Based on similar scale to that used for STO-3G energies in Table 1.

Table 3. Comparison of energies calculated using MNDO/STO-3G ( $E_{\mathrm{C}}$ ) and from rotational potentials ( $E_{\mathrm{V}}$ )

| $\theta_{1}$ | $\theta_{2}$ | $E_{\mathrm{C}}{ }^{a}$ | $E_{\mathrm{V}}{ }^{a}$ | $E_{\mathrm{C}}-E_{\mathrm{V}}$ |
| ---: | :---: | ---: | ---: | :---: |
| 0.0 | 0.0 | 67.8 | -10.8 | 78.6 |
| 36.0 | 36.0 | 4.3 | 3.3 | 1.0 |
| 60.0 | 60.0 | 17.7 | 19.8 | -2.1 |
| 90.0 | 90.0 | 29.9 | 30.0 | -0.1 |
| 0.0 | 36.0 | 27.6 | -3.8 | 31.4 |
| 0.0 | 90.0 | 9.7 | 9.6 | 0.1 |
| 36.0 | 90.0 | 16.5 | 16.6 | 0.1 |

${ }^{a}$ Based on similar scale to that used for STO-3G energies in Table 1.
large. The STO-3G study produces a more interesting result, indicating a barrier of $9.2 \mathrm{~kJ} \mathrm{~mol}^{-1}\left(2.2 \mathrm{kcal} \mathrm{mol}^{-1}\right)$, the highenergy conformer being equivalent to a helical conformer of $\theta_{1}=\theta_{2}=54^{\circ}$. Intermediate helical conformations where $\theta_{1}$ does not equal $\theta_{2}$ are predicted to be lower in energy. The perpendicular conformer previously mentioned is $3.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$ less energetic than the above high-energy form.
(iii) Rotational Potentials.--Internal rotation in molecules can be separated into one-fold ( $V_{1}$ ), two-fold ( $V_{2}$ ), and threefold $\left(V_{3}\right)$ components, ${ }^{18}$ the relative importance of each depending on the molecular structure. In benzophenone rotation of one ring around the $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ bond may be described by a simple two-fold potential, given by equation (2),

$$
\begin{equation*}
E(\theta)=V_{0}=V_{2}(1-\cos 2 \theta) / 2 \tag{2}
\end{equation*}
$$

where $E$ is the energy of a particular conformation, $\theta$ is the angle of twist from the carbonyl plane, and $V_{0}$ is a constant depending on the energy scale chosen.

In order to evaluate $V_{2}$ and $V_{0}$ a series of MNDO and STO3G calculations were performed varying $\theta_{2}$ with $\theta_{1}=90^{\circ}$, using a similar procedure to that previously described. This particular series of conformers was chosen to minimise the steric contribution to the overall energy, the MNDO optimised geometries showing the extent to which this was achieved. For example, the $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ bond length was only $0.004 \AA$ longer in the $\theta_{2}=90^{\circ}$ conformer (which might be expected to be the most sterically hindered) than in the $\theta_{2}=0^{\circ}$ conformer ( 1.511 and $1.515 \AA$, respectively). The $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ angle was $\leqslant 120.0^{\circ}$ for all conformations considered.

From the above, a value of $20.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$ for $V_{2}$ was obtained. In order to account for the simultaneous rotation of both rings, however, it is necessary to modify equation (2) as follows:

$$
E\left(\theta_{1}, \theta_{2}\right)=
$$

where $\theta_{1}$ and $\theta_{2}$ are the respective twist angles previously defined (Figure 2). In this format the value of $V_{0}$ is -10.8 kJ $\mathrm{mol}^{-1}$ for the energy scale chosen.

Equation (3) can now be used to calculate conformational energies, and these values may be compared with those obtained from MNDO/STO-3G calculations. The results (Table 3) indicate that equation (3) adequately reproduces calculated energies for conformers in which there is no significant steric contribution to the overall energy. The planar form is predicted to be the low-energy conformer, the correct result when only conjugational factors are considered. The $E_{\mathrm{C}}-E_{\mathrm{V}}$ term gives a crude approximation of the steric energy.

## Experimental

Commercial samples of benzophenone (Aldrich) and 3,4'dichlorobenzophenone (I.C.I.) were recrystallised from light petroleum (b.p. $60-80^{\circ} \mathrm{C}$ ) prior to use. The LIS experiments were carried out using the incremental weighing method in which weighed amounts of shift reagent are added to a known mass of substrate. ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ n.m.r. spectra were recorded at 250 MHz and 62.8 MHz respectively on a Bruker WM 250 spectrometer at ambient temperature. The solvent used, $\mathrm{CDCl}_{3}$, was dried over molecular sieves and the shift reagents, substrates, and all apparatus used were dried in vacuo over $\mathrm{P}_{4} \mathrm{O}_{10}$ for 24 h prior to use.

Correlation coefficients obtained from $\rho$ vs. observed shift plots for each atom were of the order $0.9980-0.9990$ for benzophenone and $0.9960-0.9970$ for $3,4^{\prime}$-dichlorobenzophenone, suggesting some deviation from linearity over the range considered ( $\rho<0.2$ ). The calculated intercept values, $\delta_{\text {INT }}$, (from the best straight line fit) shown in Tables 4 and 5 are all larger than the observed shifts of the spectra recorded at $\rho=0$ (i.e. no lanthanide shift reagent added). Furthermore, removal of the $\rho=0$ point produces an improvement in the correlation coefficients (average values $>0.9990$ for benzophenone and $>0.9980$ for $3,4^{\prime}$-dichlorobenzophenone). Both these observations indicate non-linearity at very low shift reagent concentrations ( $\rho<0.02$ ).

Exclusion of the $\rho=0$ point does not, however, significantly effect the relative $\Delta M$ values and as it is these, rather than the absolute values, which are used in the LIRAS3 analysis, inclusion of this point was considered to be justified.
(i) Results.-Observed chemical shifts ( $\delta$ ), diamagnetic shifts ( $\Delta D$ ), LISs ( $\Delta M$ ), and pseudo-contact shifts ( $\Delta M-\Delta D=\delta \Delta$ ) for benzophenone (1) are shown in Table 4 with the equivalent information for 3,4'-dichlorobenzophenone (2) given in Table 5.

Comparison of observed $\delta \Delta$ values with values calculated for various lanthanide positions and substrate conformations was carried out using the LIRAS3 programme. ${ }^{19}$ Calculation of an agreement factor, $R$, for each position and conformation allows

Table 4. Observed ${ }^{13} \mathrm{C}$ and ${ }^{1} \mathrm{H}$ shifts ( $\delta$ ), diamagnetic shifts $(\Delta D)$, intercept values ( $\delta_{\mathrm{INT}}$ ), LISs $(\Delta M)$, and pseudo-contact shifts ( $\Delta M-\Delta D$ ) for benzophenone (in p.p.m.)

|  | $\mathrm{C}-1$ | $\mathrm{C}-2$ | $\mathrm{C}-3$ | $\mathrm{C}-4$ | $\mathrm{C}=\mathrm{O}$ |
| :--- | ---: | ---: | ---: | ---: | ---: |
| $\delta^{a, b}$ | 137.63 | 129.96 | 128.22 | 132.31 | 196.56 |
| $\Delta D^{c}$ | -2.47 | 2.42 | -0.04 | 2.07 | 6.71 |
| $\delta_{\mathrm{INT}}$ | 137.90 | 130.11 | 128.27 | 132.35 | 197.19 |
| $\Delta M^{d}$ | 56.28 | 32.78 | 12.42 | 11.06 | 129.49 |
| $\Delta M-\Delta D$ | 58.75 | 30.36 | 12.46 | 8.99 | 122.78 |
|  |  |  |  |  |  |
|  | $1-\mathrm{H}$ | $2-\mathrm{H}$ | $3-\mathrm{H}$ |  |  |
| $\delta^{b}$ | 7.79 | 7.46 | 7.57 |  |  |
| $\delta_{\mathrm{INT}}$ | 7.95 | 7.49 | 7.60 |  |  |
| $\Delta M^{d}$ | 31.25 | 6.10 | 5.10 |  |  |

${ }^{a}$ Shifts referenced to $\mathrm{CDCl}_{3}$ (77.0 p.p.m.). ${ }^{b}$ Shifts from TMS. ${ }^{c}$ Three additions of $\mathrm{La}(\mathrm{fod})_{3}, \rho=0.0437,0.1284,0.1567$. ${ }^{d}$ Four additions of $\mathrm{Yb}(\text { fod })_{3}, \rho=0.0183,0.1001,0.1240,0.1864$.

Table 5. Observed ${ }^{13} \mathrm{C}$ and ${ }^{1} \mathrm{H}$ shifts ( $\delta$ ), diamagnetic shifts $(\Delta D)$, intercept values ( $\delta_{\mathrm{INT}}$ ), LISs $(\Delta M)$, and pseudo-contact shifts ( $\Delta M-\Delta D$ ) for 3,4'-dichlorobenzophenone (in p.p.m.)

|  | C-1 | C-2 | C-3 | C-4 | C-5 | C-6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\delta^{a . b}$ | 138.87 | 129.72 | 134.70 | 132.52 | 129.72 | 127.89 |
| $\Delta D^{c}$ | -1.34 | 1.14 | -0.01 | 1.34 | 0.12 | 1.45 |
| $\delta_{\text {INT }}$ | 139.16 | 129.88 | 134.76 | 132.57 | 129.77 | 128.05 |
| $\Delta M^{\text {d }}$ | 53.06 | 29.42 | 11.62 | 9.72 | 11.09 | 30.60 |
| $\Delta M-\Delta D$ | 54.40 | 28.28 | 11.63 | 8.38 | 10.97 | 29.15 |
|  | C-1' | C-2' | C-3' | C-4' | $\mathrm{C}=0$ |  |
| $\delta^{a, b}$ | 135.21 | 131.35 | 128.79 | 139.34 | 193.90 |  |
| $\Delta D^{c}$ | -1.22 | 1.47 | 0.08 | 1.88 | 4.46 |  |
| $\delta_{\text {INT }}$ | 135.50 | 131.52 | 128.85 | 139.40 | 194.54 |  |
| $\Delta M^{\text {d }}$ | 54.13 | 31.19 | 11.92 | 11.07 | 123.15 |  |
| $\Delta M-\Delta D$ | 55.35 | 29.72 | 11.84 | 9.19 | 118.69 |  |
|  | 1-H | 2-H | 3-H | 4-H | $1^{\prime}-\mathrm{H}$ | 2'-H |
| $\delta^{b}$ | 7.64 | 7.43 | 7.56 | 7.75 | 7.75 | 7.48 |
| $\delta_{\text {INT }}$ | 7.79 | 7.46 | 7.58 | 7.90 | 7.90 | 7.51 |
| $\Delta M^{d}$ | 29.18 | 5.00 | 4.53 | 26.88 | 29.87 | 5.62 |

${ }^{a}$ Shifts referenced to $\mathrm{CDCl}_{3}$ (77.0 p.p.m.). ${ }^{b}$ Shifts from TMS. ${ }^{c}$ Four additions of $\mathrm{La}(\mathrm{fod})_{3}, \rho=0.0355,0.0748,0.1335,0.1864$. ${ }^{d}$ Four additions of $\mathrm{Yb}(\text { fod })_{3}, \rho=0.0421,0.0542,0.1036,0.1393$.

(1)

(2)
an assessment of the molecular conformation in solution to be obtained.
A four-site lanthanide complexation model was used in the analysis, allowing the lanthanide site to be reflected in the xy and xz planes (Figure 6). Variation of the percentage of lanthanide complexed on either side of the carbonyl group, i.e. across the xz plane, can be carried out. However, the benzophenone molecule is symmetrical about this plane and thus equal populations were assumed. Unsymmetrical substitution of the rings destroys the plane of symmetry and requires the possibility of an uneven population distribution to be considered.
Analysis of the above data was carried out using the geometry parameters shown in Table 6. These were assumed to be unchanged for the chlorinated compound. ${ }^{8}$ Individual benzene ring planarity and $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})-\mathrm{C}\left(1^{\prime}\right)$ planarity were fürther assumed.
(a) Benzophenone. Starting from the planar form, the rings


Figure 6. Illustration of parameters used in equation (1) and the LIRAS3 analysis
were rotated in a conrotatory manner in $10^{\circ}$ increments until the $90^{\circ}$ conformer was reached. It became apparent that the number of $\delta \Delta$ values available (five ${ }^{13} \mathrm{C}$ and three ${ }^{1} \mathrm{H}$ atoms) was insufficient to produce a well determined solution, indeed all conformations produced reasonable agreement (agreement factor $R<2.0 \%$ ) for lanthanide binding sites having $\mathrm{Ln}-\mathrm{O}$ $2.75-2.85 \AA, \varphi 70-90^{\circ}, \psi 150-160^{\circ}$ and (as explained earlier) equal occupation of all sites. The problem arises because the

Table 6. Geometry parameters used in the LIRAS3 analysis

| Parameter | Value |
| :---: | :--- |
| Bond lengths $(\AA) ; \mathrm{C}=\mathrm{O}$ | $1.210^{a}$ |
| $\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ | $1.481^{a}$ |
| $\mathrm{C}-\mathrm{C}$ in ring | 1.400 |
| $\mathrm{C}-\mathrm{H}$ | 1.080 |
| $\mathrm{C}-\mathrm{C}(1)$ | $1.726^{a}$ |
|  |  |
| Bond angles $\left(^{\circ}\right) ;$ | $\mathrm{C}-\mathrm{C}(\mathrm{O})-\mathrm{C}$ |
|  | $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{C}(\mathrm{O})$ |
| $\mathrm{C}-\mathrm{C}-\mathrm{C}$ in ring | $120.9^{a}$ |
| $\mathrm{H}-\mathrm{C}-\mathrm{C}$ | 120.0 |
|  | 120.0 |
|  |  |

${ }^{a}$ Values taken from reference 10.

Table 7. Comparison of equivalent $\delta M$ values of benzophenone and $3,4^{\prime}$-dichlorobenzophenone expressed as a percentage of their respective $\delta M_{\mathrm{C}=0}$ values

| Atom type | Benzophenone |  | 3,4'-dichlorobenzophenone ${ }^{a}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\delta M$ | $\%$ of $\delta M_{\mathrm{C}=0}$ | סM | $\% \text { or } \delta M_{\mathrm{C}=0}$ |
| $\mathrm{C}=0$ | 129.5 | 100.0 | 123.2 | 100.0 |
| C-1 | 56.3 | 43.5 | 53.6 | 43.5 |
| C-2 | 32.8 | 25.3 | 30.6 | 24.8 |
| C-3 | 12.4 | 9.6 | 11.6 | 9.4 |
| C-4 | 11.1 | 8.6 | 10.4 | 8.4 |
| 1-H | 31.1 | 24.2 | 28.9 | 23.5 |

${ }^{a}$ Averaged values. Comparison of $2-\mathrm{H}$ and $3-\mathrm{H}$ is not possible due to the substituents in these positions in $3,4^{\prime}$-dichlorobenzophenone.
positions of four of the nuclei ( $\mathrm{C}-1, \mathrm{C}-4,3-\mathrm{H}$, and $\mathrm{C}_{\mathrm{C}=\mathrm{O}}$ ) are unaffected by ring rotation whilst the remaining four, whose positions do change, each have an overall LIS which is an average of the individual shifts of the equivalent nuclei on opposite sides of the ring. Thus the calculated LIS values for different conformations are unchanged for four atoms and only slightly changed for the other four atoms, making an assessment of the preferred twist angle impossible from the above analysis.
(b) 3,4'-Dichlorobenzophenone. In view of the above it was decided to use a substituted benzophenone in order to obtain a value for the twist angle in the parent molecule, assuming the substituent(s) do not significantly change the preferred conformation. For this assumption to be valid and to overcome the problems encountered above the chosen molecule had to meet certain criteria when compared to benzophenone itself; (a) a similar steric interaction between the rings, this clearly excludes ortho substitution; (b) a similar conjugative interaction between the rings, maintenance of similar $\pi$ electron density in each ring; (c) production of non-equivalence between previously equivalent atoms, both within each ring and in opposite rings, thus an unsymmetrical substitution is favoured and (d) substituent(s) must not contain a potential lanthanide-binding site.
$3,4^{\prime}$-Dichlorobenzophenone meets all the above requirements. A comparison of the $\delta M$ values for benzophenone and 3,4'-dichlorobenzophenone (Tables 4 and 5) clearly indicates a difference between the respective values for equivalent atoms. However, when each set are expressed as a percentage of their $\mathrm{C}=\mathrm{O} \delta M$ values then good agreement is obtained (Table 7). This observation indicates that the chloro substituents have no significant effect on the preferred molecular conformation and do not influence the lanthanide-substrate geometry to any great extent (the population distribution of the lanthanide between favoured sites is affected, see later). It therefore seems reasonable to assume that the preferred twist angle obtained for $3,4^{\prime}$-dichlorobenzophenone will be similar to that found in benzophenone itself.


Figure 7. Planar forms of 3,4'-dichlorobenzophenone, (a) trans and (b) cis conformations

LIRAS3 analysis was carried out in a similar way to that described for benzophenone. However, a complication arises in that there are now two possible conformations (cis and trans with respect to the meta $\mathrm{Cl} / \mathrm{C}=\mathrm{O}$ positions) for a given twist angle. Using the planar trans form as the starting point [Figure $7(\mathrm{a})]$ the twist angle was varied from $0-180^{\circ}$ (the planar cis form, Figure 7(b)] for a variety of conformer ratios. A 60:40 conformer ratio, for example, refers to a $60 \%$ trans, $40 \%$ cis distribution for twist angles $0-90^{\circ}$ and a $60 \%$ cis, $40 \%$ trans distribution for twist angles $90-180^{\circ}$.

The series of analyses described above produced, for each conformer ratio, a minimum agreement factor, $R$, at a particular twist angle and lanthanide position. The best $R$ values were found for conformer ratios in the 60:40-50:50 region, at twist angles $20-30^{\circ}$. In all these cases the position of the lanthanide was approximately the same, values of $\varphi=55-60^{\circ}$ and $\psi=$ $160-165^{\circ}$ with a $\mathrm{Ln}-\mathrm{O}$ distance of $2.75 \AA$. An uneven distribution of lanthanide was indicated, $55 \%$ being bound on the meta-chloro side of the carbonyl and $45 \%$ on the parachloro side. This observation will be considered further below.

Figure 8 shows a series of plots of agreement factor $v s$. twist angle for various conformer ratios using the above lanthanide geometry (with averaged values of $\varphi=57^{\circ}$ and $\psi=162^{\circ}$ ). In each case two minima are seen, the lower one occurring when the trans conformer predominates (twist angle $=\theta_{\text {OPT }}<90^{\circ}$ ) and the second for an angle ( $\left.180-\theta_{\mathrm{OPT}}\right)^{\circ}$ (for the $50: 50$ case the $\theta$ and $180-\theta$ conformations are equivalent). The value of $\theta_{\text {OPT }}$ decreases from $50^{\circ}$ for a 100:0 conformer ratio (not shown in Figure 8) to about $25^{\circ}$ for the $50: 50$ situation. A plot of the minima at different conformer ratios indicates that $3,4^{\prime}$ dichlorobenzophenone in chloroform exists $56 \%$ in the trans form (see Figure 9). The twist angle at this conformer ratio is $26^{\circ}$.
(ii) Discussion.-The indicated lanthanide position can be rationalised in the following manner. For the trans conformation two of the four lanthanide sites are favourable (sites 1 and 4, Figure 10) and two are unfavourable ( 2 and 3 ) if minimisation of steric interactions with the rings is considered to be the major factor in the positioning of the lanthanide, a conclusion that has been reached in many previous studies. ${ }^{20.21}$

For the cis conformation sites 2 and 3 will be favourable whilst sites 1 and 4 become unfavourable, thus, on average, all four sites will be occupied with $28 \%$ of bound lanthanide in each of sites 1 and 4 and $22 \%$ in each of 2 and 3 (the percentage occupation reflecting the presence of $56 \%$ of the trans form). This, however, assumes there is no preference for site 1 over site 4 (or vice versa) and equally for site 2 over site 3 (or vice versa). If this assumption holds then $50 \%$ of the lanthanide should be bound on each side of the carbonyl, but the LIRAS3 analysis indicated preferrential binding on the side of the meta-substituted ring ( $55 \%$ ).


Figure 8. Plots of agreement factor, $R$, vs. twist angle for various conformer ratios of $3,4^{\prime}$-dichlorobenzophenone. $\left(\mathrm{Ln}-\mathrm{O}=2.75 \AA, \varphi=57^{\circ}, \psi=\right.$ $162^{\circ} ; 55 \% \mathrm{Ln}$ on meta side of the carbonyl)


Figure 9. Plot of minimum agreement factors at various conformer ratios of $3,4^{\prime}$-dichlorobenzophenone. ( $\mathrm{Ln}-\mathrm{O}=2.75 \AA, \varphi=57^{\circ}, \psi=$ $162^{\circ} ; 55 \% \mathrm{Ln}$ on meta side of the carbonyl)

A comparison of 'equivalent' nuclei on the two rings also suggests that there must be an uneven lanthanide distribution on each side of the carbonyl group. Averaging of the $\delta \Delta$ values in the meta-chloro ring is necessary for a reasonable comparison and when this is performed the $\delta \Delta$ values of the carbon atoms in this ring are all about $2-3 \%$ smaller than the values for the corresponding carbons in the para-substituted ring. This effect is reproduced computationally for a 55:45 (meta:para) population ratio of the lanthanide. This result indicates the importance of the $3 \cos ^{2} \theta$ term in the McConnell-Robertson equation, from a simple consideration of the distance ( $r_{i}$ ) term the relative $\delta \Delta$ values indicate an excess of lanthanide on the para-chloro ring side of the carbonyl.

The uneven distribution of the lanthanide across the carbonyl group is most reasonably attributed to slight differences in the $\pi$ electron density in the respective rings. A further consideration may be a degree of electrostatic attraction to the meta-chloro atom when the substrate is bound in the cis conformation. However, the lanthanide to chlorine distance is large so this is perhaps unlikely.

The combination of steric effects combined with conformational preferences (i.e. trans vs. cis) in solution and $\pi$ density differences in the two rings results in unequal occupation of all four sites, the percentage of lanthanide in each being $25 \%$ (site 1 ), $24 \%$ (site 2), $20 \%$ (site 3 ), and $31 \%$ (site 4 ), see Figure 10 . Thus site 4 is the most favoured binding site since it is sterically


Figure 10. Lanthanide-binding sites in $3,4^{\prime}$-dichlorobenzophenone
favoured in the trans conformer and is also situated on the metachloro ring side of the carbonyl. Conversely site 3 is sterically favoured when the molecule is in the less abundant cis conformation and is situated on the para-chloro ring side of the carbonyl. Hence site 3 is the least occupied binding site. Application of the same arguments to sites 1 and 2 shows them to meet one of the two conditions for a favoured site and one of the two conditions for an unfavoured site, this being reflected in their percentage occupation being intermediate between those of site 3 and site 4 .

## Conclusions

Comparison of the relative $\delta M$ values for benzophenone and 3,4'-dichlorobenzophenone shown in Table 7 indicates that the meta and para substituents exert no significant effect on the preferred conformation. The difference in the absolute values is most likely to be due to small variations in the experimental conditions rather than any change of lanthanide-binding site brought about by conformational changes in the substituted compound.

The theoretical value of $\theta$ predicted using an STO-3G basis set in GAUSSIAN76 $\left(36^{\circ}\right)$ is in reasonable agreement with the experimentally derived value ( $26^{\circ}$ ) and both methods produce figures similar to those obtained in previous studies. The trans conformer of $3,4^{\prime}$-dichlorobenzophenone was found to be the predominant form in solution ( $56 \%: 44 \%$ ), however, attempts to relate this to the respective energies of the cis and trans conformers were unsuccessful, MNDO calculating them to be of the same energy and the presence of the chloro substituents making the molecule too large to be used in GAUSSIAN76.

The theoretical calculations indicated that MNDO alone cannot correctly predict conformational preferences in conjugated systems. The combination of MNDO optimised geometries and STO-3G energies seems to be a reasonable
approach to this problem. A comparison of Figures 4 and 5 suggests that ring rotation will occur via a disrotatory mechanism (MNDO predicts the conrotatory mechanism to be more likely) and the calculated energy of the $\theta_{1}=0^{\circ}$, $\theta_{2}=90^{\circ}$ conformer ( $9.7 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ) indicates that it might be the high-energy intermediate of the pathway.

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